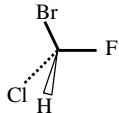
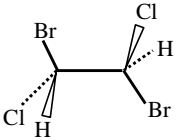
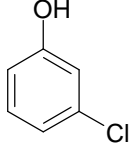
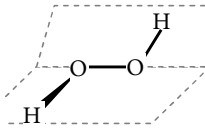
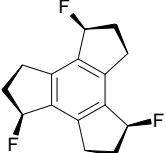
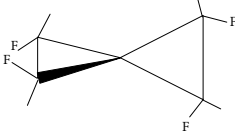
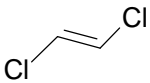
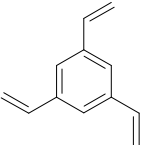
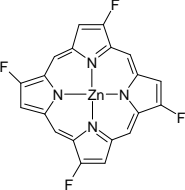
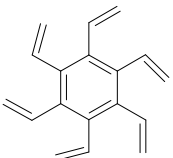
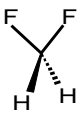
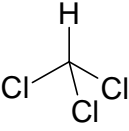
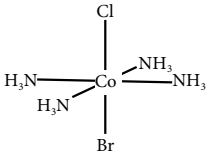
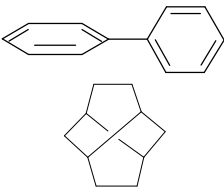


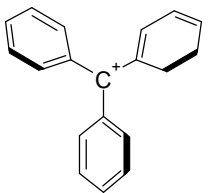
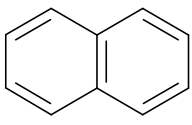
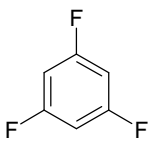
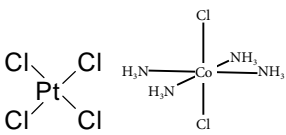



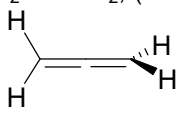
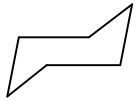

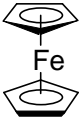
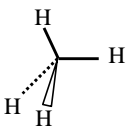
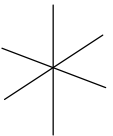
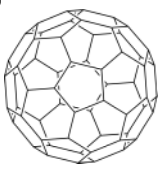
# Examples of point groups, character tables and comparison of Schönflies & Hermann-Mauguin (or International) term symbols.

## Examples of some Point Groups

(from Beddard, Applying Maths in the Chemical & Biomolecular Sciences', p338)

Most of the H atoms are not included on the structures.

<p><math>C_1</math> CHClFBr, cholesterol</p> 	<p><math>C_i</math> staggered 1,2-dibromo-1,2-dichloroethane</p> 	<p><math>C_s</math> meta-chlorophenol, <math>\text{HN}_3</math></p> 
<p><math>C_2</math> <math>\text{H}_2\text{O}_2</math></p> 	<p><math>C_3</math></p> 	<p><math>S_4</math></p> 
<p><math>C_{2h}</math> trans <math>\text{ClHC=CHCl}</math></p> 	<p><math>C_{3h}</math> 1,3,5-trivinylbenzene (if planar)</p> 	<p><math>C_{4h}</math> tetra fluoroZn-porphyrin</p> 
<p><math>C_{6h}</math> hexa-vinylbenzene (if planar)</p> 	<p><math>C_{2v}</math> <math>\text{H}_2\text{O}</math>, <math>\text{COCl}_2</math>, <math>\text{CH}_2\text{F}_2</math>, <math>\text{CF}_2\text{C=CH}_2</math>, pyridine (<math>\text{C}_5\text{H}_5\text{N}</math>)</p> 	<p><math>C_{3v}</math> <math>\text{NH}_3</math>, <math>\text{CHCl}_3</math>, <math>\text{OPF}_3</math></p> 
<p><math>C_{4v}</math> <math>\text{B}_5\text{H}_9</math>, <math>\text{SF}_5\text{Cl}</math></p> 	<p><math>C_{\infty v}</math> HF and all other heteronuclear diatomics,</p> <p><math>\text{HCN}</math>, <math>\text{F-C}\equiv\text{C-H}</math></p>	<p><math>D_2</math> twisted biphenyl, twistane.</p> 

$D_3$ triphenylmethane <sup>+</sup> ion (propeller shaped) 	$D_{2h}$ CH <sub>2</sub> =CH <sub>2</sub> , Naphthalene 	$D_{3h}$ BF <sub>3</sub> , C <sub>3</sub> H <sub>3</sub> , 1, 3, 5- trifluorobenzene 
$D_{4h}$ PtCl <sub>4</sub> <sup>2-</sup> 	$D_{5h}$ C <sub>5</sub> H <sub>5</sub> <sup>-</sup> , IF <sub>7</sub> , Ru(C <sub>5</sub> H <sub>5</sub> ) <sub>2</sub> 	$D_{6h}$ Benzene 
$D_{7h}$ Tropylium ion C <sub>7</sub> H <sub>7</sub> <sup>-</sup> . 	$D_{2d}$ CH <sub>2</sub> =C=CH <sub>2</sub> , (allene) 	$D_{3d}$ staggered ethane, chair cyclohexane 
$D_{4d}$ crown S <sub>8</sub> , B <sub>10</sub> H <sub>10</sub> <sup>2-</sup> , (no H are shown, B atom at each apex) 	$D_{5d}$ Ferrocene 	$D_{\infty h}$ H <sub>2</sub> and all other homonuclear diatomics,  F-C≡C-F, C <sub>2</sub> N <sub>2</sub> , CO <sub>2</sub>
$T_d$ (Tetrahedral) CH <sub>4</sub> , CF <sub>4</sub> 	$O_h$ (octahedral) SF <sub>6</sub> , cubane, Fe(CN) <sub>6</sub> <sup>4-</sup> 	$I_h$ (icosahedral) B <sub>12</sub> H <sub>12</sub> <sup>2-</sup> , C <sub>60</sub> , football, 

## Simple comparison of common point groups

$C_n$   $n$ -fold rotation axis only.

$C_{nv}$   $n$ -fold rotation with axis *parallel* to  $n$  mirror planes.

$C_{nh}$   $n$ -fold rotation with axis *perpendicular* (normal) to a mirror plane.

$D_n$   $n$ -fold axis and at least one perpendicular 2-fold axis. No mirror planes.

$D_{nd}$  same as  $D_n$  plus mirror planes bisecting 2-fold axes.

$S_4$ ,  $S_6$  2 fold & 3 fold rotation inversion respectively. ( $S_2 \equiv i$ ).

$T$ ,  $T_d$ ,  $T_h$  2 & 3 fold rotation axes.

$O$ ,  $O_h$  2, 3 & 4 fold rotation axes.

$I_h$  2, 3, & 5 fold rotation axes.

## Point Groups and their Symmetry Operations (excluding the identity E).

$C_n \equiv 360^\circ/n$  fold rotation;  $n = 2 \equiv 180^\circ$ ;  $n = 3 \equiv 120^\circ$ ;  $n = 4 \equiv 90^\circ$  rotation.  $i =$  inversion,

$\sigma_h =$  horizontal mirror plane,  $\sigma_v =$  vertical mirror,  $\sigma_d =$  dihedral mirror plane. Angle is  $360^\circ/n$ .

$S_n =$  rotation-reflection.  $C_n^2$  means  $C_n$  applied twice over,  $S_n^5$  means  $S_n$  applied 5 times etc.

**Note that for 3, 4, 5, 6 etc. axes, but not 2-fold axes ( $C_2$ ), an entry such as  $8C_3$  indicates that there are only four  $C_3$  axes, with half of the operations clockwise rotation and half anti-clockwise.**

( Note also that  $C_n^n = E$ ,  $S_2 = i$ ,  $S_{2n}^n = C_n$  )

### Symmetry Operations

Point group	$C_2$	$C_3$	$C_{4,5,6,8}$	$i$	$\sigma_v$	$\sigma_h$	$\sigma_d$	$S_n$	<i>all the rest (excluding identity E, except <math>C_1</math>)</i>
$C_1$									$E$ (identity only)
$C_s$						$\sigma_h$			
$C_i$				$i$					
$C_2$	$C_2$								
$C_3$		$C_3$							$C_3^2$
$C_{2v}$	$C_2$				$\sigma_v, \sigma_{v'}$				
$C_{3v}$		$2C_3$			$3\sigma_v$				
$C_{4v}$	$C_2$		$2C_4$		$2\sigma_v$		$2\sigma_d$		
$C_{5v}$			$2C_5$		$5\sigma_v$				$2C_5^2$
$C_{6v}$	$C_2$	$2C_3$	$C_6$		$3\sigma_v$		$3\sigma_d$		
$C_{2h}$	$C_2$			$i$		$\sigma_h$			
$C_{3h}$		$C_3$				$\sigma_h$		$S_3$	$C_3^2, S_3^5$
$C_{4h}$	$C_2$		$C_4$	$i$		$\sigma_h$		$S_4$	$C_4^3, S_4^3$
$C_{6h}$	$C_2$	$C_3$	$C_6$	$i$		$\sigma_h$		$S_6$	$S_3, S_3^5, S_6^5, C_3^2, C_6^5$
$D_2$	$3C_2$								$C_2 \equiv C_2(x), C_2(y), C_2(z)$
$D_3$	$3C_2$	$2C_3$							
$D_4$	$C_2$		$2C_4$						$2C_2', C_2''$
$D_{2h}$	$3C_2$			$i$	$2\sigma_v$	$\sigma_h$			$\sigma \equiv \sigma(xy), \sigma(xz), \sigma(yz)$
$D_{3h}$	$3C_2$	$2C_3$			$3\sigma_v$	$\sigma_h$		$2S_3$	
$D_{4h}$	$C_2$		$2C_4$	$i$	$2\sigma_v$	$\sigma_h$	$2\sigma_d$	$2S_4$	$2C_2', 2C_2''$
$D_{5h}$	$5C_2$		$5C_5$		$5\sigma_v$	$\sigma_h$		$2S_5$	$2C_5^2$
$D_{6h}$	$C_2$	$2C_3$	$2C_6$	$i$	$3\sigma_v$	$\sigma_h$	$3\sigma_d$	$2S_6$	$3C_2', 3C_2'', 2S_3,$
$D_{8h}$	$C_2$		$2C_8$	$i$	$4\sigma_v$	$\sigma_h$	$4\sigma_d$	$2S_8$	$4C_2', 4C_2'', 2C_4, C_8^3, 2S_8,$ $2S_8^3$
$D_{2d}$	$C_2$						$2\sigma_d$	$2S_4$	$2C_2'$
$D_{3d}$	$3C_2$	$2C_3$		$i$			$3\sigma_d$	$2S_6$	
$D_{4d}$	$C_2$		$2C_4$				$4\sigma_d$	$2S_8$	$4C_2', 2S_8^3$
$D_{5d}$	$5C_2$		$2C_5$	$i$			$5\sigma_d$	$2S_{10}$	$2C_5^2, 2S_{10}^3$
$S_4$	$C_2$							$S_4$	$S_4^3$
$S_6$		$C_3$		$i$				$S_6$	$C_3^2, S_6^5$
$T$	$3C_2$	$4C_3$							$4C_3^2$
$T_d$	$3C_2$	$8C_3$					$6\sigma_d$	$6S_4$	
$T_h$	$3C_2$	$4C_3$		$i$		$3\sigma_h$		$4S_6$	$4C_3^2, 4S_6^5$
$O$	$3C_2$	$8C_3$	$6C_4$						$6C_2,$
$O_h$	$6C_2$	$8C_3$	$6C_4$	$i$		$3\sigma_h$	$6\sigma_d$	$6S_4$	$8S_6, 3C_2$
$I_h$	$15C_2$	$20C_3$	$12C_5$	$i$			$15\sigma$	$12S_{10}$	$20S_6, 12S_{10}^3, 12C_5^2$

Identify  $D_{\infty h}$  (e.g. homonuclear diatomic) and  $C_{\infty v}$  (e.g. heteronuclear diatomic) directly by their shape.

## Character tables

$C_1$	$E$
$A$	1

$C_i$	$E$	$i$		
$A_g$	1	1	$R_x, R_y, R_z$	$x^2, y^2, z^2, xy, xz, yz$
$A_u$	1	-1	$x, y, z$	

$C_s$	$E$	$\sigma_h$		
$A'$	1	1	$x, y, R_z$	$x^2, y^2, z^2, xy$
$A''$	1	-1	$z, R_x, R_y$	$yz, xz$

$C_2$	$E$	$C_2$		
$A$	1	1	$z, R_z$	$x^2, y^2, z^2, xy$
$B$	1	-1	$x, y, R_x, R_y$	$xz, yz$

$C_3$	$E$	$C_3$	$C_3^2$	$\varepsilon = e^{2\pi i/3}$	
$A$	1	1	1	$z, R_z$	$x^2 + y^2$
$E$	{	1	$\varepsilon$	$\varepsilon^*$	(x, y),
		1	$\varepsilon^*$	$\varepsilon$	(R <sub>x</sub> , R <sub>y</sub> )
				}	(x <sup>2</sup> - y <sup>2</sup> , xy), (xz, yz)

$C_4$	$E$	$C_4$	$C_2$	$C_4^3$		
$A$	1	1	1	1	$z, R_z$	$x^2 + y^2, z^2$
$B$	1	-1	1	-1		$x^2 - y^2, xy$
$E$	$\left\{ \begin{array}{l} 1 \\ 1 \end{array} \right.$	$\left\{ \begin{array}{l} i \\ -i \end{array} \right.$	$\left\{ \begin{array}{l} -1 \\ -1 \end{array} \right.$	$\left\{ \begin{array}{l} -i \\ i \end{array} \right.$	$(x, y), (R_x, R_y)$	$(xz, yz)$

$C_5$	$E$	$C_5$	$C_5^2$	$C_5^3$	$C_5^4$	$\varepsilon = e^{2\pi i/5}$	
$A$	1	1	1	1	1	$z, R_z$	$x^2 + y^2, z^2$
$E_1$	$\left\{ \begin{array}{l} 1 \\ 1 \end{array} \right.$	$\left\{ \begin{array}{l} \varepsilon \\ \varepsilon^* \end{array} \right.$	$\left\{ \begin{array}{l} \varepsilon^2 \\ \varepsilon^{2*} \end{array} \right.$	$\left\{ \begin{array}{l} \varepsilon^{2*} \\ \varepsilon^2 \end{array} \right.$	$\left\{ \begin{array}{l} \varepsilon^* \\ \varepsilon \end{array} \right.$	$(x, y), (R_x, R_y)$	$(xz, yz)$
$E_2$	$\left\{ \begin{array}{l} 1 \\ 1 \end{array} \right.$	$\left\{ \begin{array}{l} \varepsilon^2 \\ \varepsilon^{2*} \end{array} \right.$	$\left\{ \begin{array}{l} \varepsilon^* \\ \varepsilon \end{array} \right.$	$\left\{ \begin{array}{l} \varepsilon \\ \varepsilon^* \end{array} \right.$	$\left\{ \begin{array}{l} \varepsilon^{2*} \\ \varepsilon^2 \end{array} \right.$		$(x^2 - y^2, xy)$

$C_6$	$E$	$C_6$	$C_3$	$C_2$	$C_3^2$	$C_6^5$	$\varepsilon = e^{2\pi i/6}$	
$A$	1	1	1	1	1	1	$z, R_z$	$x^2 + y^2, z^2$
$B$	1	-1	1	-1	1	-1		
$E_1$	$\left\{ \begin{array}{l} 1 \\ 1 \end{array} \right.$	$\left\{ \begin{array}{l} \varepsilon \\ \varepsilon^* \end{array} \right.$	$\left\{ \begin{array}{l} -\varepsilon^* \\ -\varepsilon \end{array} \right.$	$\left\{ \begin{array}{l} -1 \\ -1 \end{array} \right.$	$\left\{ \begin{array}{l} -\varepsilon \\ -\varepsilon^* \end{array} \right.$	$\left\{ \begin{array}{l} \varepsilon^* \\ -\varepsilon \end{array} \right.$	$(x, y), (R_x, R_y)$	$(xz, yz)$
$E_2$	$\left\{ \begin{array}{l} 1 \\ 1 \end{array} \right.$	$\left\{ \begin{array}{l} -\varepsilon^* \\ -\varepsilon \end{array} \right.$	$\left\{ \begin{array}{l} -\varepsilon \\ -\varepsilon^* \end{array} \right.$	$\left\{ \begin{array}{l} 1 \\ 1 \end{array} \right.$	$\left\{ \begin{array}{l} -\varepsilon^* \\ -\varepsilon \end{array} \right.$	$\left\{ \begin{array}{l} -\varepsilon \\ -\varepsilon^* \end{array} \right.$		$(x^2 - y^2, xy)$

$C_8$	$E$	$C_8$	$C_4$	$C_2$	$C_4^3$	$C_8^3$	$C_8^5$	$C_8^7$	$\varepsilon = e^{2\pi i/8}$	
$A$	1	1	1	1	1	1	1	1	$z, R_z$	$x^2 + y^2, z^2$
$B$	1	-1	1	1	1	-1	-1	-1	$(x, y), (R_x, R_y)$	$(xz, yz)$
$E_1$	1	$\varepsilon$	$i$	-1	- $i$	- $\varepsilon^*$	- $\varepsilon$	$\varepsilon^*$		
	1	$\varepsilon^*$	- $i$	-1	$i$	- $\varepsilon$	- $\varepsilon^*$	$\varepsilon$		
$E_2$	1	$i$	-1	1	-1	- $i$	$i$	- $i$	$(x^2 - y^2, xy)$	
	1	- $i$	-1	1	-1	$i$	- $i$	$i$		
$E_3$	1	- $\varepsilon^*$	$i$	-1	- $i$	$\varepsilon^*$	$\varepsilon$	- $\varepsilon^*$		
	1	- $\varepsilon$	- $i$	-1	$i$	$\varepsilon$	$\varepsilon^*$	- $\varepsilon$		

$D_2$	$E$	$C_2(z)$	$C_2(x)$	$C_2(y)$		
$A$	1	1	1	1		$x^2, y^2, z^2$
$B_1$	1	1	-1	-1	$z, R_z$	$xy$
$B_2$	1	-1	-1	1	$y, R_y$	$xz$
$B_3$	1	-1	1	-1	$x, R_x$	$yz$

$D_3$	$E$	$2C_3$	$3C_2$		
$A_1$	1	1	1		$x^2 + y^2, z^2$
$A_2$	1	1	-1	$z, R_z$	
$E$	2	-1	0	$(x, y), (R_x, R_y)$	$(x^2 - y^2, xy), (xz, yz)$

$D_4$	$E$	$2C_4$	$C_2$	$2C_2'$	$2C_2''$		
$A_1$	1	1	1	1	1		$x^2 + y^2, z^2$
$A_2$	1	1	1	-1	-1	$z, R_z$	
$B_1$	1	-1	1	1	-1		$x^2 - y^2$
$B_2$	1	-1	1	-1	1		$xy$
$E$	2	0	-2	0	0	$(x, y), (R_x, R_y)$	$(xz, yz)$

$D_5$	$E$	$2C_5$	$2C_5^2$	$5C_2$	$\theta = 2\pi/5 \equiv 72^\circ$	
$A_1$	1	1	1	1	$(x, y), (R_x, R_y)$	$x^2 + y^2, z^2$
$A_2$	1	1	1	-1		$z, R_z$
$E_1$	2	$2 \cos(\theta)$	$2 \cos(2\theta)$	0		$(xz, yz)$
$E_2$	2	$2 \cos(2\theta)$	$2 \cos(\theta)$	0		$(x^2 - y^2, xy)$

$S_4$	$E$	$S_4$	$C_2$	$S_4^3$				
$A$	1	1	1	1	$R_z,$	$x^2 + y^2, z^2$		
$B$	1	-1	1	-1	$z$	$x^2 - y^2, xy$		
$E$	}	1	$i$	-1	$-i$	}	$(x, y), (R_x, R_y)$	$(xz, yz)$
		1	$-i$	-1	$i$			

$S_6$	$E$	$C_3$	$C_3^2$	$i$	$S_6^5$	$S_6$	$\varepsilon = \varepsilon^{2\pi i/6}$		
$A_g$	1	1	1	1	1	1	$R_z$	$x^2 + y^2, z^2$	
$E_g$	}	1	$\varepsilon$	$\varepsilon^*$	1	$\varepsilon$	$\varepsilon^*$	}	$(x^2 - y^2, xy), (xz, yz)$
		1	$\varepsilon^*$	$\varepsilon$	1	$\varepsilon^*$	$\varepsilon$		
$A_u$	1	1	1	-1	-1	-1	$z$		
$E_u$	}	1	$\varepsilon$	$\varepsilon^*$	-1	$-\varepsilon$	$-\varepsilon^*$	}	$(x, y)$
		1	$\varepsilon^*$	$\varepsilon$	-1	$-\varepsilon^*$	$-\varepsilon$		

$C_{2v}$	$E$	$C_2$	$\sigma_v(xz)$	$\sigma_v'(yz)$		
$A_1$	1	1	1	1	$z$	$x^2, y^2, z^2$
$A_2$	1	1	-1	-1	$R_z$	$xy$
$B_1$	1	-1	1	-1	$x, R_y$	$xz$
$B_2$	1	-1	-1	1	$y, R_x$	$yz$

$C_{3v}$	$E$	$2C_3$	$3\sigma_v$		
$A_1$	1	1	1	$z$	$x^2 + y^2, z^2$
$A_2$	1	1	-1	$R_z$	
$E$	2	-1	0	$(x, y), (R_x, R_y)$	$(x^2 - y^2, xy), (xz, yz)$

$C_{4v}$	$E$	$2C_4$	$C_2$	$2\sigma_v$	$2\sigma_d$		
$A_1$	1	1	1	1	1	$z$	$x^2 + y^2, z^2$
$A_2$	1	1	1	-1	-1	$R_z$	
$B_1$	1	-1	1	1	-1		$x^2 - y^2$
$B_2$	1	-1	1	-1	1		$xy$
$E$	2	0	-2	0	0	$(x, y), (R_x, R_y)$	$(xz, yz)$

$C_{5v}$	$E$	$2C_5$	$2C_5^2$	$5\sigma_v$	$\theta = 2\pi/5 \equiv 72^\circ$	
$A_1$	1	1	1	1	$z$	$x^2 + y^2, z^2$
$A_2$	1	1	1	-1	$R_z$	
$E_1$	2	$2\cos(\theta)$	$2\cos(2\theta)$	0	$(x, y), (R_x, R_y)$	$(xz, yz)$
$E_2$	2	$2\cos(2\theta)$	$2\cos(\theta)$	0		$(x^2 - y^2, xy)$



$C_{6v}$	$E$	$2C_6$	$2C_3$	$C_2$	$3\sigma_v$	$3\sigma_d$		
$A_1$	1	1	1	1	1	1	$z$	$x^2 + y^2, z^2$
$A_2$	1	1	1	1	-1	-1	$R_z$	
$B_1$	1	-1	1	-1	1	-1		
$B_2$	1	-1	1	-1	-1	1		
$E_1$	2	1	-1	-2	0	0	$(R_x, R_y), (x, y)$	$(xz, yz)$
$E_2$	2	-1	-1	2	0	0		$(x^2 - y^2, xy)$

$C_{2h}$	$E$	$C_2$	$i$	$\sigma_h$		
$A_g$	1	1	1	1	$R_z$	$x^2, y^2, z^2, xy$
$B_g$	1	-1	1	-1	$R_x, R_y$	$xz, yz$
$A_u$	1	1	-1	-1	$z$	
$B_u$	1	-1	-1	1	$x, y$	

$C_{3h}$	$E$	$C_3$	$C_3^2$	$\sigma_h$	$S_3$	$S_3^5$	$\varepsilon = e^{2\pi i/3}$			
$A'$	1	1	1	1	1	1	$R_z$	$x^2 + y^2, z^2$		
$E'$	}	1	$\varepsilon$	$\varepsilon^*$	1	$\varepsilon$	$\varepsilon^*$	}	$(x, y)$	$(x^2 - y^2, xy)$
		1	$\varepsilon^*$	$\varepsilon$	1	$\varepsilon^*$	$\varepsilon$			
$A''$	}	1	1	1	-1	-1	-1	}	$z$	
		1	1	1	-1	-1	-1			
$E''$	}	1	$\varepsilon$	$\varepsilon^*$	-1	$-\varepsilon$	$-\varepsilon^*$	}	$(R_x, R_y)$	$(xz, yz)$
		1	$\varepsilon^*$	$\varepsilon$	-1	$-\varepsilon^*$	$-\varepsilon$			

$C_{4h}$	$E$	$C_4$	$C_2$	$C_4^3$	$i$	$S_4^3$	$\sigma_h$	$S_4$		
$A_g$	1	1	1	1	1	1	1	1	$R_z$	$x^2 + y^2, z^2$
$B_g$	1	-1	1	-1	1	-1	1	-1		$x^2 - y^2, xy$
$E_g$	}	1	$i$	-1	$-i$	1	$i$	-1	$(R_x, R_y)$	$(xz, yz)$
		1	$-i$	-1	$i$	1	$-i$	-1	$i$	
$A_u$	1	1	1	1	-1	-1	-1	-1	$z$	
$B_u$	1	-1	1	-1	-1	1	-1	1		
$E_u$	}	1	$i$	-1	$-i$	-1	$-i$	1	$(x, y)$	$(x, y)$
		1	$-i$	-1	$i$	-1	$i$	1	$-i$	

$C_{5h}$	$E$	$C_5$	$C_5^2$	$C_5^3$	$C_5^4$	$\sigma_h$	$S_5$	$S_5^7$	$S_5^3$	$S_5^9$	$\varepsilon = e^{2\pi i/5}$		
$A'$	1	1	1	1	1	1	1	1	1	1	$R_z$	$x^2 + y^2, z^2$	
$E_1'$	}	1	$\varepsilon$	$\varepsilon^2$	$\varepsilon^{2*}$	$\varepsilon^*$	1	$\varepsilon$	$\varepsilon^2$	$\varepsilon^{2*}$	$\varepsilon^*$	$(x, y)$	
		1	$\varepsilon^*$	$\varepsilon^{2*}$	$\varepsilon^2$	$\varepsilon$	1	$\varepsilon^*$	$\varepsilon^{2*}$	$\varepsilon^2$	$\varepsilon$		
$E_2'$	}	1	$\varepsilon^2$	$\varepsilon^*$	$\varepsilon$	$\varepsilon^{2*}$	1	$\varepsilon^2$	$\varepsilon^*$	$\varepsilon$	$\varepsilon^{2*}$	$(x^2 - y^2, xy)$	
		1	$\varepsilon^{2*}$	$\varepsilon$	$\varepsilon^*$	$\varepsilon^2$	1	$\varepsilon^{2*}$	$\varepsilon$	$\varepsilon^*$	$\varepsilon^2$		
$A''$	1	1	1	1	1	-1	-1	-1	-1	-1	$z$		
$E_1''$	}	1	$\varepsilon$	$\varepsilon^2$	$\varepsilon^{2*}$	$\varepsilon^*$	-1	$-\varepsilon$	$-\varepsilon^2$	$-\varepsilon^{2*}$	$-\varepsilon^*$	$(R_x, R_y)$	$(xz, yz)$
		1	$\varepsilon^*$	$\varepsilon^{2*}$	$\varepsilon^2$	$\varepsilon$	-1	$-\varepsilon^*$	$-\varepsilon^{2*}$	$-\varepsilon^2$	$-\varepsilon$		
$E_2''$	}	1	$\varepsilon^2$	$\varepsilon^*$	$\varepsilon$	$\varepsilon^{2*}$	-1	$-\varepsilon^2$	$-\varepsilon^*$	$-\varepsilon$	$-\varepsilon^{2*}$	$(x, y)$	
		1	$\varepsilon^{2*}$	$\varepsilon$	$\varepsilon^*$	$\varepsilon^2$	-1	$-\varepsilon^{2*}$	$-\varepsilon$	$-\varepsilon^*$	$-\varepsilon^2$		

$C_{6h}$	$E$	$C_6$	$C_3$	$C_2$	$C_3^2$	$C_6^5$	$i$	$S_3^5$	$S_6^5$	$\sigma_h$	$S_6$	$S_3$	$\varepsilon = e^{2\pi i/6}$			
$A_g$	1	1	1	1	1	1	1	1	1	1	1	1	$R_z$	$x^2 + y^2, z^2$		
$B_g$	1	-1	1	-1	1	-1	1	-1	1	-1	1	-1				
$E_{1g}$	}	1	$\varepsilon$	$-\varepsilon^*$	-1	$-\varepsilon$	$\varepsilon^*$	1	$\varepsilon$	$-\varepsilon^*$	-1	$-\varepsilon$	$\varepsilon^*$	}	$(R_x, R_y)$	$(xz, yz)$
		1	$\varepsilon^*$	$-\varepsilon$	-1	$-\varepsilon^*$	$\varepsilon$	1	$\varepsilon^*$	$-\varepsilon$	-1	$-\varepsilon^*$	$\varepsilon$			
$E_{2g}$	}	1	$-\varepsilon^*$	$-\varepsilon$	1	$-\varepsilon^*$	$-\varepsilon$	1	$-\varepsilon^*$	$-\varepsilon$	1	$-\varepsilon^*$	$-\varepsilon$	}		$(x^2 - y^2, xy)$
		1	$-\varepsilon$	$-\varepsilon^*$	1	$-\varepsilon$	$-\varepsilon^*$	1	$-\varepsilon$	$-\varepsilon^*$	1	$-\varepsilon$	$-\varepsilon^*$			
$A_u$	1	1	1	1	1	1	-1	-1	-1	-1	-1	-1	$z$			
$B_u$	1	-1	1	-1	1	-1	-1	1	-1	1	-1	1				
$E_{1u}$	}	1	$\varepsilon$	$-\varepsilon^*$	-1	$-\varepsilon$	$\varepsilon^*$	-1	$-\varepsilon$	$\varepsilon^*$	1	$\varepsilon$	$-\varepsilon^*$	}	$(x, y)$	
		1	$\varepsilon^*$	$-\varepsilon$	-1	$-\varepsilon^*$	$\varepsilon$	-1	$-\varepsilon^*$	$\varepsilon$	1	$\varepsilon^*$	$-\varepsilon$			
$E_{2u}$	}	1	$-\varepsilon^*$	$-\varepsilon$	1	$-\varepsilon^*$	$-\varepsilon$	-1	$\varepsilon^*$	$\varepsilon$	-1	$\varepsilon^*$	$\varepsilon$	}		
		1	$-\varepsilon$	$-\varepsilon^*$	1	$-\varepsilon$	$-\varepsilon^*$	-1	$\varepsilon$	$\varepsilon^*$	-1	$\varepsilon$	$\varepsilon^*$			

$D_{2h}$	$E$	$C_2(z)$	$C_2(y)$	$C_2(x)$	$i$	$\sigma(xy)$	$\sigma(xz)$	$\sigma(yz)$		
$A_g$	1	1	1	1	1	1	1	1	$x^2, y^2, z^2$	
$B_{1g}$	1	1	-1	-1	1	1	-1	-1	$R_z$	$xy$
$B_{2g}$	1	-1	1	-1	1	-1	1	-1	$R_y$	$xz$
$B_{3g}$	1	-1	-1	1	1	-1	-1	1	$R_x$	$yz$
$A_u$	1	1	1	1	-1	-1	-1	-1		
$B_{1u}$	1	1	-1	-1	-1	-1	1	1	$z$	
$B_{2u}$	1	-1	1	-1	-1	1	-1	1	$y$	
$B_{3u}$	1	-1	-1	1	-1	1	1	-1	$x$	

$D_{3h}$	$E$	$2C_3$	$3C_2$	$\sigma_h$	$2S_3$	$3\sigma_v$		
$A_1'$	1	1	1	1	1	1	$R_z$	$x^2 + y^2, z^2$
$A_2'$	1	1	-1	1	1	-1		
$E'$	2	-1	0	2	-1	0	$(x, y)$	$(x^2 - y^2, xy)$
$A_1''$	1	1	1	-1	-1	-1		
$A_2''$	1	1	-1	-1	-1	1	$z$	
$E''$	2	-1	0	-2	1	0	$(R_x, R_y)$	$(xz, yz)$

$D_{4h}$	$E$	$2C_4$	$C_2$	$2C_2'$	$2C_2''$	$i$	$2S_4$	$\sigma_h$	$2\sigma_v$	$2\sigma_d$		
$A_{1g}$	1	1	1	1	1	1	1	1	1	1	$R_z$	$x^2 + y^2, z^2$
$A_{2g}$	1	1	1	-1	-1	1	1	1	-1	-1		
$B_{1g}$	1	-1	1	1	-1	1	-1	1	1	-1		$x^2 - y^2$
$B_{2g}$	1	-1	1	-1	1	1	-1	1	-1	1		$xy$
$E_g$	2	0	-2	0	0	2	0	-2	0	0	$(R_x, R_y)$	$(xz, yz)$
$A_{1u}$	1	1	1	1	1	-1	-1	-1	-1	-1		
$A_{2u}$	1	1	1	-1	-1	-1	-1	-1	1	1	$z$	
$B_{1u}$	1	-1	1	1	-1	-1	1	-1	-1	1		
$B_{2u}$	1	-1	1	-1	1	-1	1	-1	1	-1		
$E_u$	2	0	-2	0	0	-2	0	2	0	0	$(x, y)$	

$D_{5h}$	$E$	$2C_5$	$2C_5^2$	$5C_2$	$\sigma_h$	$2S_5$	$2S_5^3$	$5\sigma_v$	$\theta=2\pi/5 \equiv 72^\circ$	
$A_1'$	1	1	1	1	1	1	1	1	$R_z$	$x^2 + y^2, z^2$
$A_2'$	1	1	1	-1	1	1	1	-1		
$E_1'$	2	$2\cos(\theta)$	$2\cos(2\theta)$	0	2	$2\cos(\theta)$	$2\cos(2\theta)$	0	$(x, y)$	
$E_2'$	2	$2\cos(2\theta)$	$2\cos(\theta)$	0	2	$2\cos(2\theta)$	$2\cos(\theta)$	0		
$A_1''$	1	1	1	1	-1	-1	-1	-1	$z$	
$A_2''$	1	1	1	-1	-1	-1	-1	1		
$E_1''$	2	$2\cos(\theta)$	$2\cos(2\theta)$	0	-2	$-2\cos(\theta)$	$-2\cos(2\theta)$	0	$(R_x, R_y)$	$(xz, yz)$
$E_2''$	2	$2\cos(2\theta)$	$2\cos(\theta)$	0	-2	$-2\cos(2\theta)$	$-2\cos(\theta)$	0		

$D_{6h}$	$E$	$2C_6$	$2C_3$	$C_2$	$3C_2'$	$3C_2''$	$i$	$2S_3$	$2S_6$	$\sigma_h$	$3\sigma_d$	$3\sigma_v$		
$A_{1g}$	1	1	1	1	1	1	1	1	1	1	1	1	$R_z$	$x^2 + y^2, z^2$
$A_{2g}$	1	1	1	1	-1	-1	1	1	1	1	-1	-1		
$B_{1g}$	1	-1	1	-1	1	-1	1	-1	1	-1	1	-1	$(R_x, R_y)$	$(xz, yz)$
$B_{2g}$	1	-1	1	-1	-1	1	1	-1	1	-1	-1	1		
$E_{1g}$	2	1	-1	-2	0	0	2	1	-1	-2	0	0	$z$	
$E_{2g}$	2	-1	-1	2	0	0	2	-1	-1	2	0	0		
$A_{1u}$	1	1	1	1	1	1	-1	-1	-1	-1	-1	-1	$(x, y)$	
$A_{2u}$	1	1	1	1	-1	-1	-1	-1	-1	-1	1	1		
$B_{1u}$	1	-1	1	-1	1	-1	-1	1	-1	1	-1	1	$(x, y)$	
$B_{2u}$	1	-1	1	-1	-1	1	-1	1	-1	1	1	-1		
$E_{1u}$	2	1	-1	-2	0	0	-2	-1	1	2	0	0		
$E_{2u}$	2	-1	-1	2	0	0	-2	1	1	-2	0	0		

$D_{8h}$	$E$	$2C_8$	$2C_4$	$2C_8^3$	$C_2$	$4C_2'$	$4C_2''$	$i$	$2S_8^3$	$2S_8$	$2S_4$	$\sigma_h$	$4\sigma_d$	$4\sigma_v$				
$A_{1g}$	1	1	1	1	1	1	1	1	1	1	1	1	1	1	$R_z$	$x^2 + y^2, z^2$		
$A_{2g}$	1	1	1	1	1	-1	-1	1	1	1	1	1	-1	-1				
$B_{1g}$	1	-1	1	-1	1	1	-1	1	-1	-1	1	1	1	-1				
$B_{2g}$	1	-1	1	-1	1	-1	1	1	-1	-1	1	1	-1	1				
$E_{1g}$	2	$\sqrt{2}$	0	$-\sqrt{2}$	-2	0	0	2	$\sqrt{2}$	$-\sqrt{2}$	0	-2	0	0			$(R_x, R_y)$	$(xz, yz)$ $(x^2 - y^2, xy)$
$E_{2g}$	2	0	-2	0	2	0	0	2	0	0	-2	2	0	0				
$E_{3g}$	2	$-\sqrt{2}$	0	$\sqrt{2}$	-2	0	0	2	$-\sqrt{2}$	$\sqrt{2}$	0	-2	0	0				
$A_{1u}$	1	1	1	1	1	1	1	-1	-1	-1	-1	-1	-1	-1	$z$			
$A_{2u}$	1	1	1	1	1	-1	-1	-1	-1	-1	-1	-1	1	1				
$B_{1u}$	1	-1	1	-1	1	1	-1	-1	1	1	-1	-1	-1	1				
$B_{2u}$	1	-1	1	-1	1	-1	1	-1	1	1	-1	-1	1	-1				
$E_{1u}$	2	$\sqrt{2}$	0	$-\sqrt{2}$	-2	0	0	-2	$-\sqrt{2}$	$\sqrt{2}$	0	2	0	0			$(x, y)$	
$E_{2u}$	2	0	-2	0	2	0	0	-2	0	0	2	-2	0	0				
$E_{3u}$	2	$-\sqrt{2}$	0	$\sqrt{2}$	-2	0	0	-2	$\sqrt{2}$	$-\sqrt{2}$	0	2	0	0				

$D_{2d}$	$E$	$2S_4$	$C_2$	$2C_2'$	$2\sigma_d$			
$A_1$	1	1	1	1	1	$R_z$	$x^2, y^2, z^2$	
$A_2$	1	1	1	-1	-1			
$B_1$	1	-1	1	1	-1		$x^2 - y^2$	
$B_2$	1	-1	1	-1	1		$z$	$xy$
$E$	2	0	-2	0	0		$(x, y), (R_x, R_y)$	$(xz, yz)$

$D_{3d}$	$E$	$2C_3$	$3C_2$	$i$	$2S_6$	$3\sigma_d$			
$A_{1g}$	1	1	1	1	1	1	$R_z$	$x^2 + y^2, z^2$	
$A_{2g}$	1	1	-1	1	1	-1			
$E_g$	2	-1	0	2	-1	0		$(R_x, R_y)$	$(x^2 - y^2, xy), (xz, yz)$
$A_{1u}$	1	1	1	-1	-1	-1			
$A_{2u}$	1	1	-1	-1	-1	1		$z$	
$E_u$	2	-1	0	-2	1	0		$(x, y)$	

$D_{4d}$	$E$	$2S_8$	$2C_4$	$2S_8^3$	$C_2$	$4C_2'$	$4\sigma_d$			
$A_1$	1	1	1	1	1	1	1	$R_z$	$x^2 + y^2, z^2$	
$A_2$	1	1	1	1	1	-1	-1			
$B_1$	1	-1	1	-1	1	1	-1			
$B_2$	1	-1	1	-1	1	-1	1		$z$	
$E_1$	2	$\sqrt{2}$	0	$-\sqrt{2}$	-2	0	0		$(x, y)$	
$E_2$	2	0	-2	0	2	0	0			$(x^2 - y^2, xy)$
$E_3$	2	$-\sqrt{2}$	0	$\sqrt{2}$	-2	0	0		$(R_x, R_y)$	$(xz, yz)$

$D_{5d}$	$E$	$2C_5$	$2C_5^2$	$5C_2$	$i$	$2S_{10}$	$2S_{10}^3$	$5\sigma_d$	$\theta = 2\pi/5 \equiv 72^\circ$	
$A_{1g}$	1	1	1	1	1	1	1	1		$x^2 + y^2, z^2$
$A_{2g}$	1	1	1	-1	1	1	1	-1	$R_z$	
$E_{1g}$	2	$2 \cos(\theta)$	$2 \cos(2\theta)$	0	2	$2 \cos(2\theta)$	$2 \cos(\theta)$	0	$(R_x, R_y)$	$(xz, yz)$
$E_{2g}$	2	$2 \cos(2\theta)$	$2 \cos(\theta)$	0	2	$2 \cos(\theta)$	$2 \cos(2\theta)$	0		$(x^2 - y^2, xy)$
$A_{1u}$	1	1	1	1	-1	-1	-1	-1		
$A_{2u}$	1	1	1	-1	-1	-1	-1	1	$z$	
$E_{1u}$	2	$2 \cos(\theta)$	$2 \cos(2\theta)$	0	-2	$-2 \cos(2\theta)$	$-2 \cos(\theta)$	0	$(x, y)$	
$E_{2u}$	2	$2 \cos(2\theta)$	$2 \cos(\theta)$	0	-2	$-2 \cos(\theta)$	$-2 \cos(2\theta)$	0		

$T$	$E$	$4C_3$	$4C_3^2$	$3C_2$	$\varepsilon = e^{2\pi i/3}$	
$A$	1	1	1	1		$x^2 + y^2 + z^2$
$E$	$\left\{ \begin{array}{l} 1 \\ 1 \end{array} \right.$	$\left\{ \begin{array}{l} \varepsilon \\ \varepsilon^* \end{array} \right.$	$\left\{ \begin{array}{l} \varepsilon^* \\ \varepsilon \end{array} \right.$	$\left\{ \begin{array}{l} 1 \\ 1 \end{array} \right.$		$(2z^2 - x^2 - y^2, x^2 - y^2)$
$T$	3	0	0	-1	$(x, y, z), (R_x, R_y, R_z)$	$(xy, xz, yz)$

$T_h$	$E$	$4C_3$	$4C_3^2$	$3C_2$	$i$	$4S_6$	$4S_6^5$	$3\sigma_h$	$\varepsilon = e^{2\pi i/3}$	
$A_g$	1	1	1	1	1	1	1	1		$x^2 + y^2 + z^2$
$A_u$	1	1	1	1	-1	-1	-1	-1		
$E_g$	$\left\{ \begin{array}{l} 1 \\ 1 \end{array} \right.$	$\left\{ \begin{array}{l} \varepsilon \\ \varepsilon^* \end{array} \right.$	$\left\{ \begin{array}{l} \varepsilon^* \\ \varepsilon \end{array} \right.$	$\left\{ \begin{array}{l} 1 \\ 1 \end{array} \right.$	$\left\{ \begin{array}{l} 1 \\ 1 \end{array} \right.$	$\left\{ \begin{array}{l} \varepsilon \\ \varepsilon^* \end{array} \right.$	$\left\{ \begin{array}{l} \varepsilon^* \\ \varepsilon \end{array} \right.$	$\left\{ \begin{array}{l} 1 \\ 1 \end{array} \right.$		$(2z^2 - x^2 - y^2, x^2 - y^2)$
$E_u$	$\left\{ \begin{array}{l} 1 \\ 1 \end{array} \right.$	$\left\{ \begin{array}{l} \varepsilon \\ \varepsilon^* \end{array} \right.$	$\left\{ \begin{array}{l} \varepsilon^* \\ \varepsilon \end{array} \right.$	$\left\{ \begin{array}{l} 1 \\ 1 \end{array} \right.$	$\left\{ \begin{array}{l} -1 \\ -1 \end{array} \right.$	$\left\{ \begin{array}{l} -\varepsilon \\ -\varepsilon^* \end{array} \right.$	$\left\{ \begin{array}{l} -\varepsilon^* \\ -\varepsilon \end{array} \right.$	$\left\{ \begin{array}{l} -1 \\ -1 \end{array} \right.$		
$T_g$	3	0	0	-1	3	0	0	-1	$(R_x, R_y, R_z)$	$(xy, xz, yz)$
$T_u$	3	0	0	-1	-3	0	0	1	$(x, y, z)$	



$T_d$	$E$	$8C_3$	$3C_2$	$6S_4$	$6\sigma_d$		
$A_1$	1	1	1	1	1		$x^2 + y^2 + z^2$
$A_2$	1	1	1	-1	-1		
$E$	2	-1	2	0	0		$(2z^2 - x^2 - y^2, x^2 - y^2)$
$T_1$	3	0	-1	1	-1	$(R_x, R_y, R_z)$	
$T_2$	3	0	-1	-1	1	$(x, y, z)$	$(xy, xz, yz)$

$O$	$E$	$6C_4$	$3C_2(=C_4^2)$	$8C_3$	$6C_2$		
$A_1$	1	1	1	1	1		$x^2 + y^2 + z^2$
$A_2$	1	-1	1	1	-1		
$E$	2	0	2	-1	0		$(2z^2 - x^2 - y^2, x^2 - y^2)$
$T_1$	3	1	-1	0	-1	$(R_x, R_y, R_z), (x, y, z)$	
$T_2$	3	-1	-1	0	1		$(xy, xz, yz)$

$O_h$	$E$	$8C_3$	$6C_2$	$6C_4$	$3C_2(=C_4^2)$	$i$	$6S_4$	$8S_6$	$3\sigma_h$	$6\sigma_d$		
$A_{1g}$	1	1	1	1	1	1	1	1	1	1		$x^2 + y^2 + z^2$
$A_{2g}$	1	1	-1	-1	1	1	-1	1	1	-1		
$E_g$	2	-1	0	0	2	2	0	-1	2	0		$(2z^2 - x^2 - y^2, x^2 - y^2)$
$T_{1g}$	3	0	-1	1	-1	3	1	0	-1	-1	$(R_x, R_y, R_z)$	
$T_{2g}$	3	0	1	-1	-1	3	-1	0	-1	1		$(xy, xz, yz)$
$A_{1u}$	1	1	1	1	1	-1	-1	-1	-1	-1		
$A_{2u}$	1	1	-1	-1	1	-1	1	-1	-1	1		
$E_u$	2	-1	0	0	2	-2	0	1	-2	0		
$T_{1u}$	3	0	-1	1	-1	-3	-1	0	1	1	$(x, y, z)$	
$T_{2u}$	3	0	1	-1	-1	-3	1	0	1	-1		

$I_h$	$E$	$12C_5$	$12C_5^2$	$20C_3$	$15C_2$	$i$	$12S_{10}$	$12S_{10}^3$	$20S_6$	$15\sigma$	$\varepsilon = \pi/5 \equiv 36^\circ$	
$A_g$	1	1	1	1	1	1	1	1	1	1		$x^2 + y^2 + z^2$
$T_{1g}$	3	$2 \cos(\varepsilon)$	$2 \cos(3\varepsilon)$	0	-1	3	$2 \cos(3\varepsilon)$	$2 \cos(\varepsilon)$	0	-1	$(R_x, R_y, R_z)$	
$T_{2g}$	3	$2 \cos(3\varepsilon)$	$2 \cos(\varepsilon)$	0	-1	3	$2 \cos(\varepsilon)$	$2 \cos(3\varepsilon)$	0	-1		
$G_g$	4	-1	-1	1	0	4	-1	-1	1	0		
$H_g$	5	0	0	-1	1	5	0	0	-1	1		§
$A_u$	1	1	1	1	1	-1	-1	-1	-1	-1		
$T_{1u}$	3	$2 \cos(\varepsilon)$	$2 \cos(3\varepsilon)$	0	-1	-3	$-2 \cos(3\varepsilon)$	$-2 \cos(\varepsilon)$	0	1	$(x, y, z)$	
$T_{2u}$	3	$2 \cos(3\varepsilon)$	$2 \cos(\varepsilon)$	0	-1	-3	$-2 \cos(\varepsilon)$	$-2 \cos(3\varepsilon)$	0	1		
$G_u$	4	-1	-1	1	0	-4	1	1	-1	0		
$H_u$	5	0	0	-1	1	-5	0	0	1	-1		

$$\S = (2z^2 - x^2 - y^2, x^2 - y^2, xy, xz, yz)$$

Comparison of Schönflies (Sc) & Hermann-Mauguin (or International) term symbols.

Sc:	$C_n$	$C_1$	$C_2$	$C_3$	$C_4$	$C_5$	$C_6$	$C_8$
H-M:		1	2	3	4	5	6	8
Sc:		$C_i$	$C_s$	$S_6 (C_{3i})$	$S_4$			
H-M:		$\bar{1}$	m ( $\equiv \bar{2}$ )	$\bar{3}$	$\bar{4}$			
Sc:	$C_{nh}$		$C_{2h}$	$C_{3h}$	$C_{4h}$	$C_{5h}$	$C_{6h}$	$C_{8h}$
H-M:			2/m	3/m ( $\equiv \bar{6}$ )	4/m	5/m ( $\equiv \bar{10}$ )	6/m	8/m
Sc:	$C_{nv}$		$C_{2v}$	$C_{3v}$	$C_{4v}$	$C_{5v}$	$C_{6v}$	$C_{8v}$
H-M:			mm2	3m	mm4	5m	mm6	mm8
Sc:	$D_n$		$D_2$	$D_3$	$D_4$	$D_5$	$D_6$	$D_8$
H-M:			222	32	422	52	622	822
Sc:	$D_{nd}$		$D_{2d}$	$D_{3d}$	$D_{4d}$	$D_{5d}$		
H-M:			$\bar{4} 2m$	$\bar{3} m$	$\bar{8} 2m$	$\bar{5} m$		
Sc:	$D_{nh}$		$D_{2h}$	$D_{3h}$	$D_{4h}$	$D_{5h}$	$D_{6h}$	$D_{8h}$
H-M:			2/mmm ( $\equiv mmm$ )	$\bar{6} m2 (\equiv 3/mm)$	4/mmm	$\bar{10} m2$	6/mmm	8/mmm
Sc:		$T$	$T_h$	$O$	$T_d$	$O_h$	$I_h$	
H-M:		23	m $\bar{3}$	432	$\bar{4} 3m$	m $\bar{3} m$	$\bar{5} \bar{3} m$	

(after Borchardt-Ott, Crystallography - An introduction, Springer, p127)